

Testing the tooth root fatigue strength of gears using resonance testing machines

60th anniversary of RUMUL Russenberger Prüfmaschinen AG

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LEHRSTUHL FÜR
ANTRIEBSTECHNIK

Chair of Drive Technology (ante)

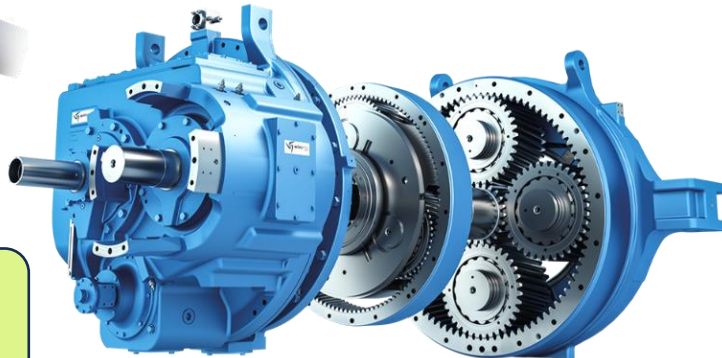


Research on Gears – but why?

Industrial Applications

- Gearboxes convert torque and rotational speed within the drivetrain

Goal 2030:
~ 10-15 % reduction in kerosene consumption



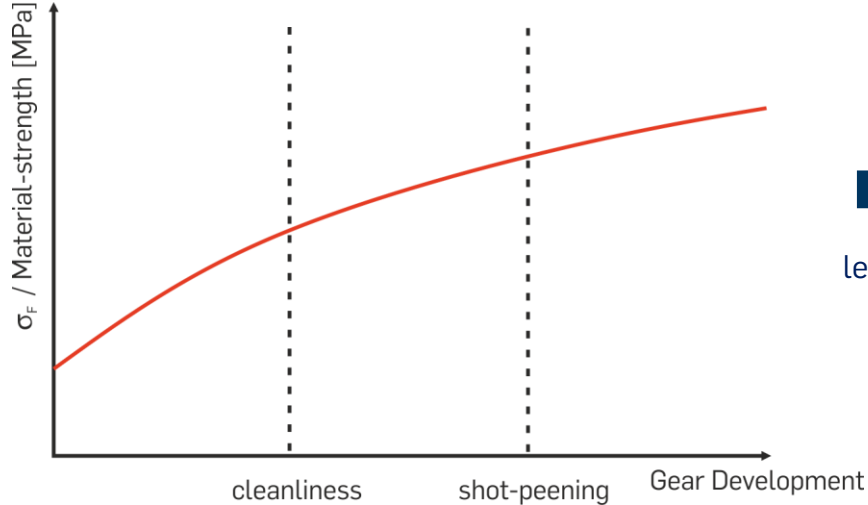
Goal: 2030
> 20 MW power in Off-shore applications



Research on Gears – but why?

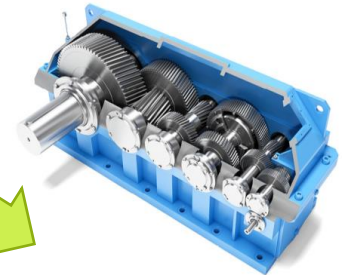
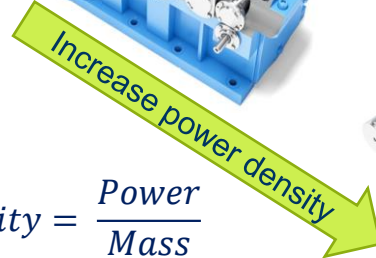
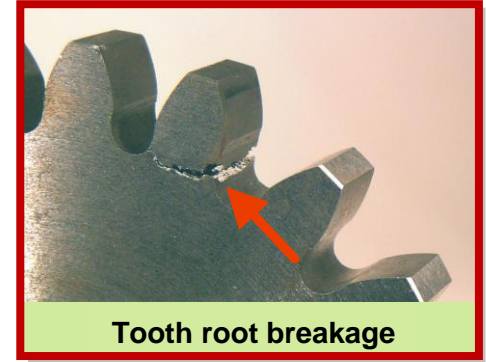
Increase the tooth root strength

- to increase power density for gearboxes
- to increase the service life of gearboxes



leads to..

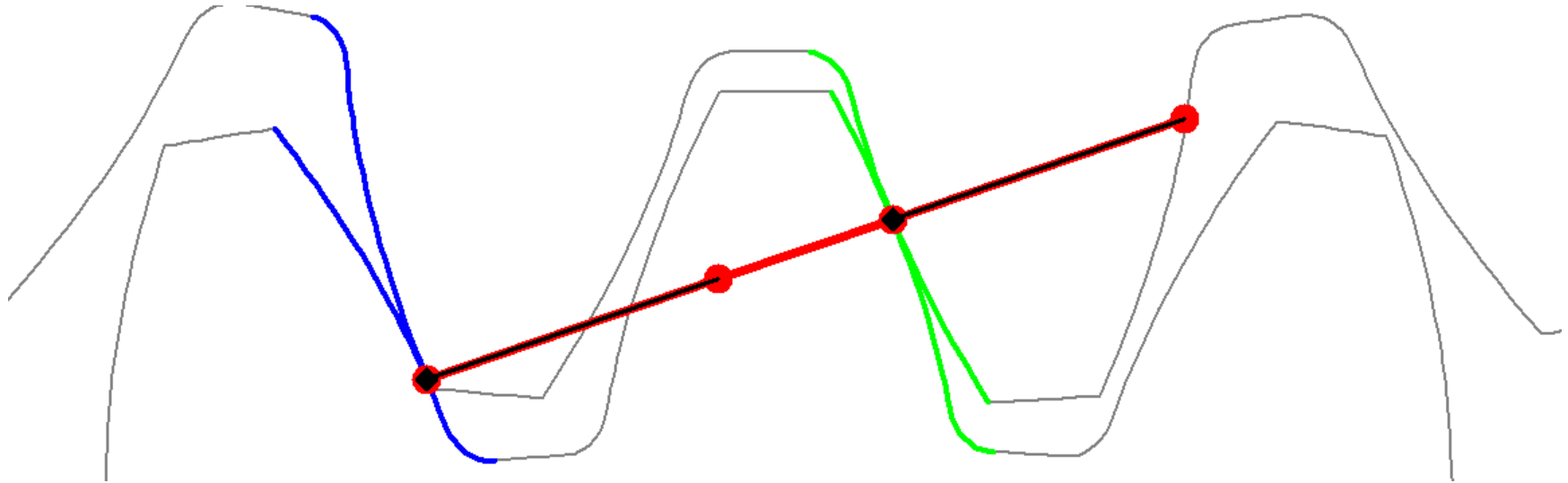
$$\text{power density} = \frac{\text{Power}}{\text{Mass}}$$



Source: www.eisenbeiss.at

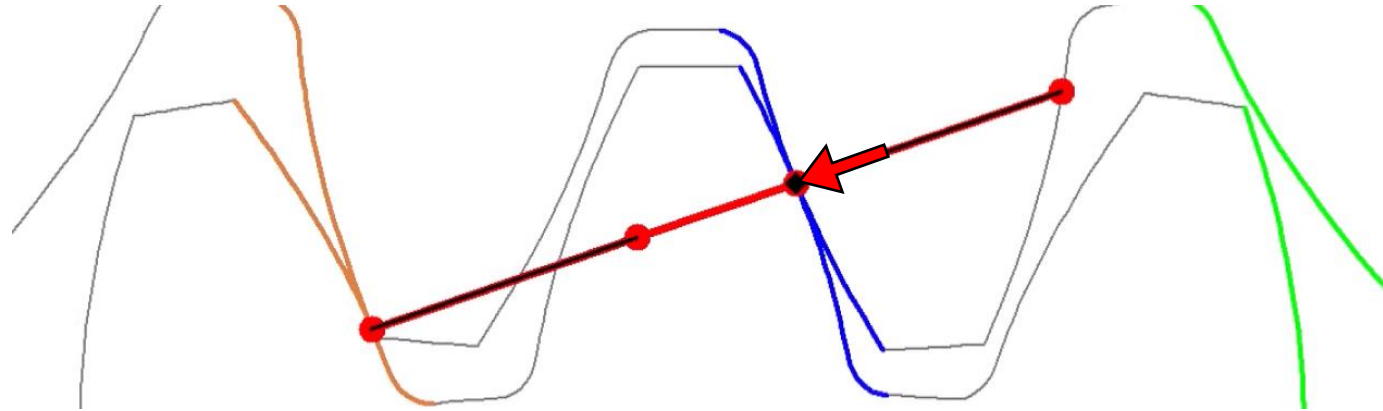
Tooth root stress

- Meshing of involute gears – origin of tooth root stresses



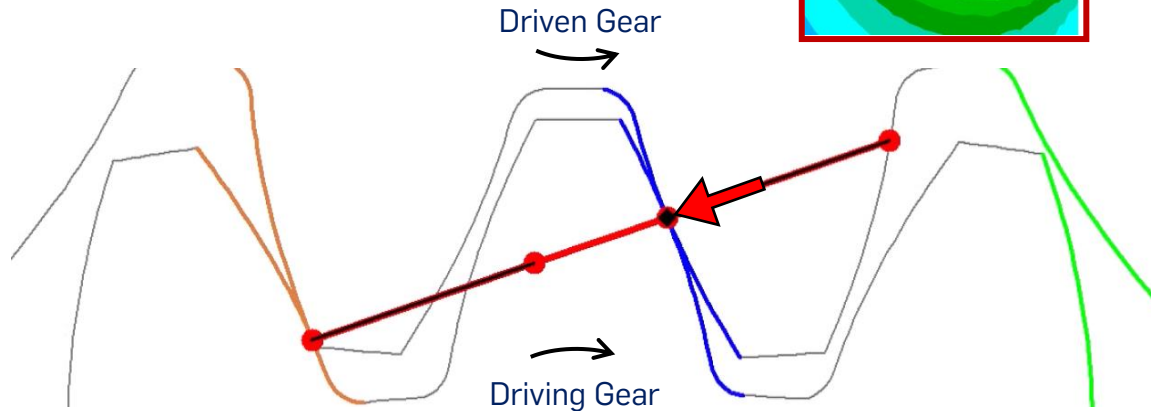
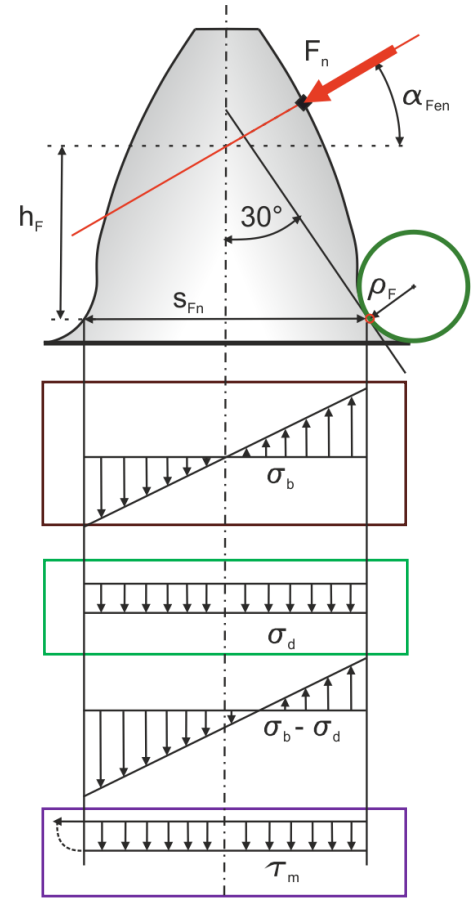
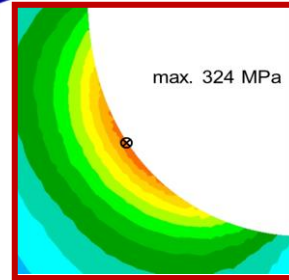
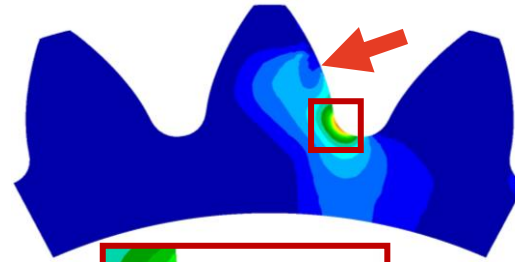
Tooth root stress

- Several stress types in the tooth root summing up to a multistate stress
 - Tensile/compressive stress
 - Bending stress
 - Shear stress



Tooth root stress

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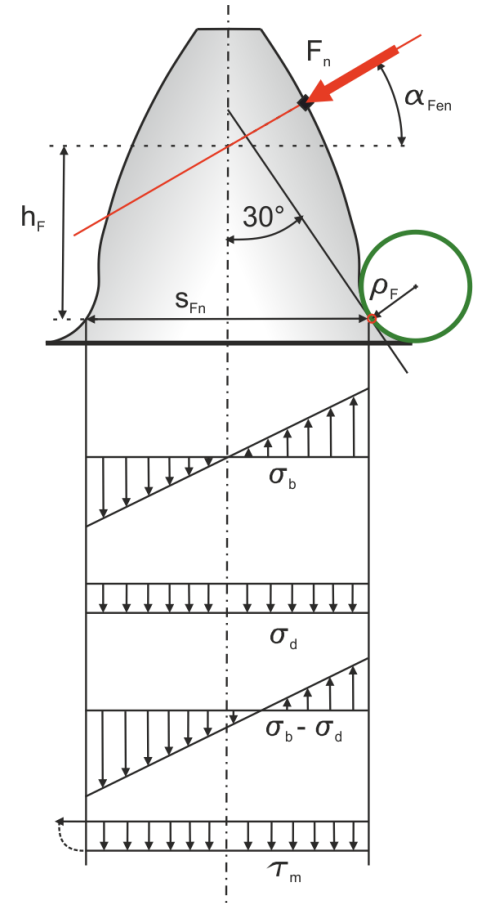
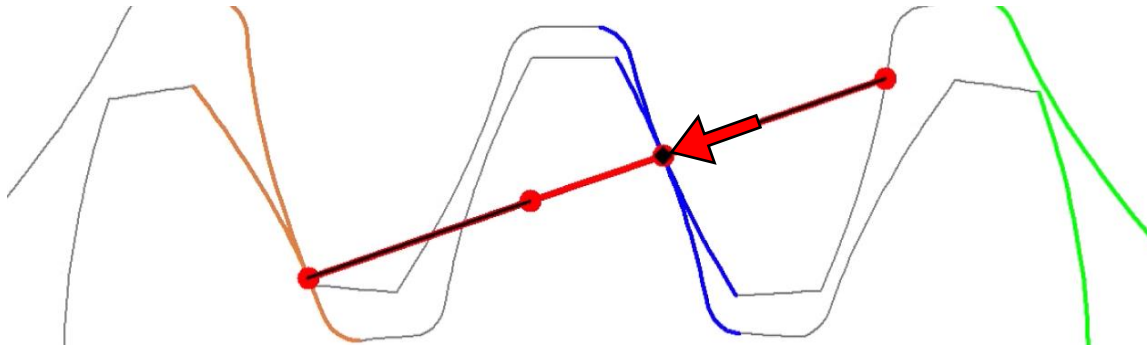
Tooth root stress

- Calculation of the tooth root bending strength σ_F acc. to ISO 6336-3

$$Y_F \cdot Y_S \cdot Y_\beta \cdot \frac{F_n \cdot \cos(\alpha_n)}{b \cdot m_n} \cdot K_A \cdot K_V \cdot K_{F\alpha} \cdot K_{F\beta} < \sigma_F \cdot Y_{ST} \cdot Y_{NT} \cdot Y_{\delta rel T} \cdot Y_{R rel T} \cdot Y_X$$

↓ Geometry ↓ Load ↓ Application ↓ Material
(Tooth bending stress)

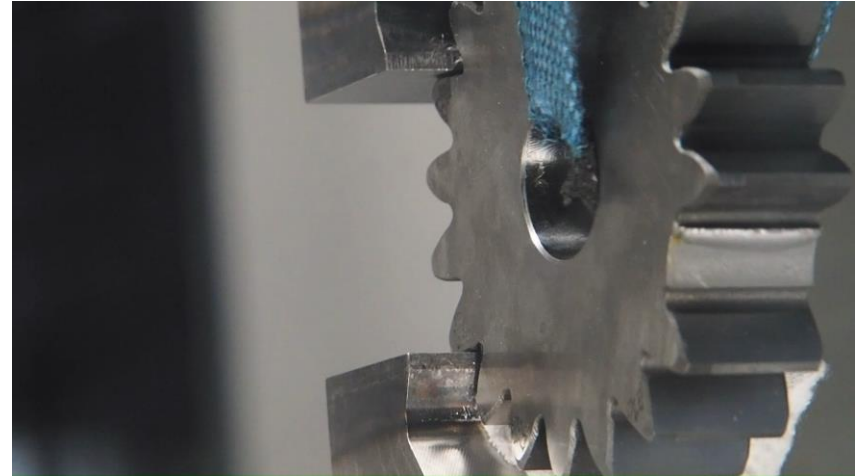
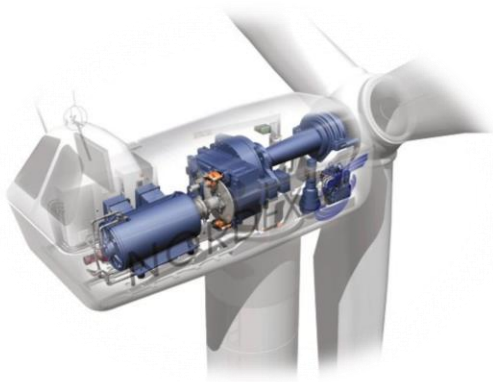
Why is the tooth root bending strength σ_F for the gear design that important?



Tooth root fatigue strength

Significance of the tooth root bending strength

- Failure of the tooth root of a gear = fatigue damage type
- Gears have to sustain high number of load cycles ($> 10^6$)



How can the tooth root bending strength be tested?

Tooth root fatigue strength

Fatigue strength testing

- Fatigue life analysis: design of components that can withstand a given external load for a specific time

Running test



Pulsator test



Tooth root fatigue strength

Fatigue strength testing

- Fatigue life analysis: design of components that can withstand a given external load for a specific time

Running test



Pulsator test

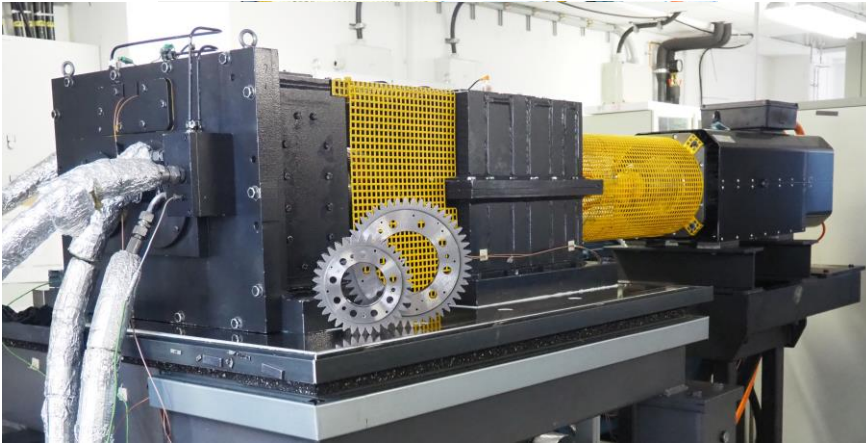


Tooth root fatigue strength

Fatigue strength testing

- Fatigue life analysis: design of components that can withstand a given external load for a specific time

Running test



Pulsator test



Tooth root fatigue strength

Fatigue strength testing

- Fatigue life analysis: design of components that can withstand a given external load for a specific time

Running test



$$N = 6 \cdot 10^6$$



$$n_{\text{pulsator}} = 100 \text{ Hz}$$

$$n_{\text{running}} = 1500 \text{ rpm} = 25 \text{ Hz}$$



$$t_{\text{pulsator}} = 16.6 \text{ H}$$

$$t_{\text{running}} = 66.6 \text{ H}$$

Pulsator test



Tooth root fatigue strength

Fatigue strength testing

- Fatigue life analysis: design of components that can withstand a given external load for a specific time

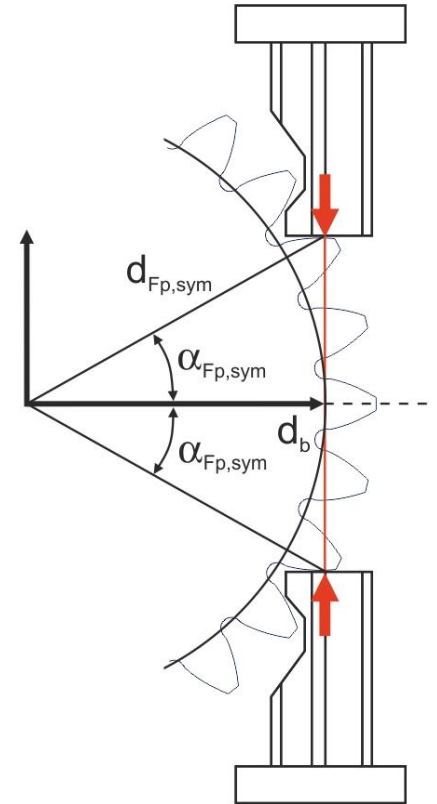
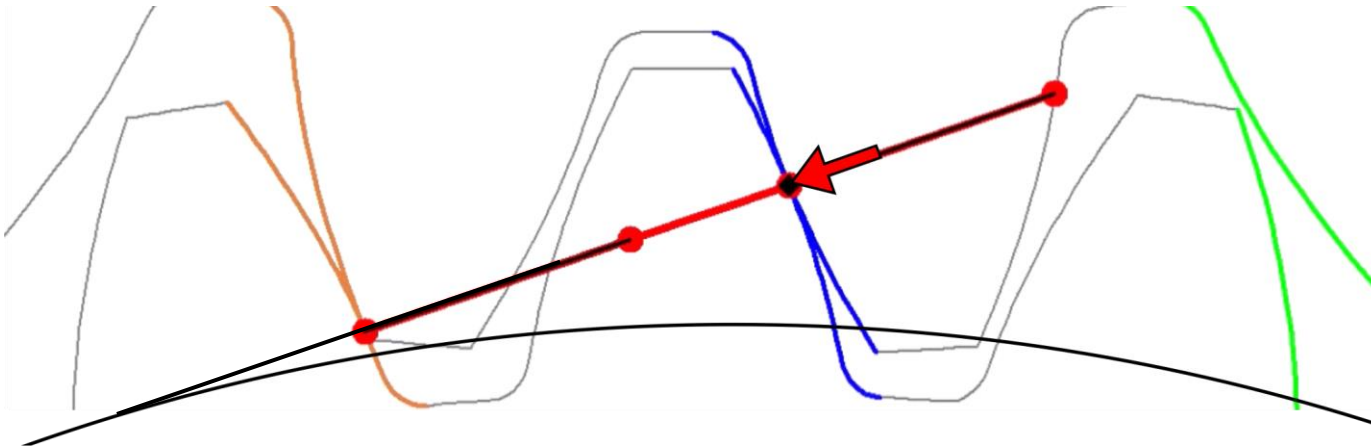


Is it possible to mount a gear into a pulsator machine?

Tooth root fatigue strength

Involute Function

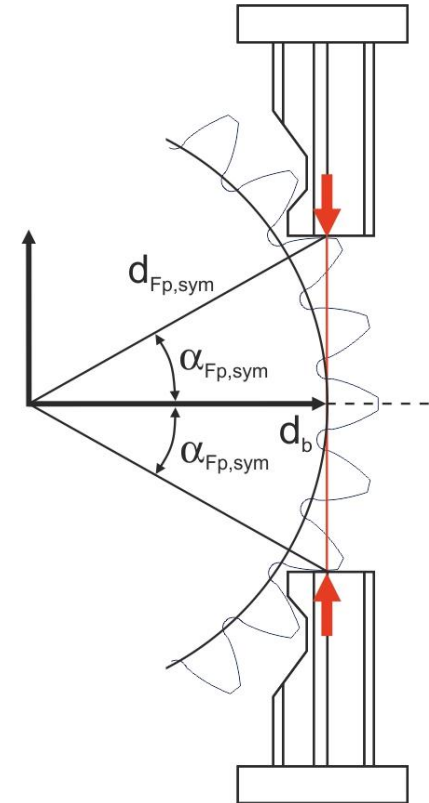
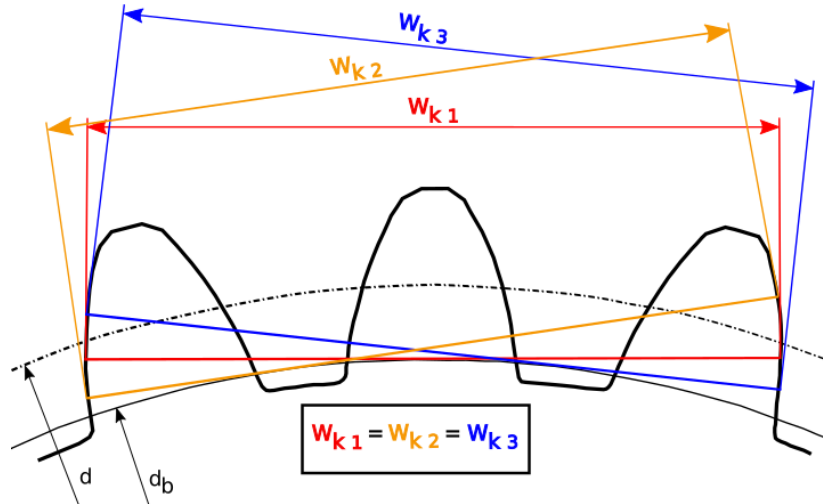
- How can we clamp a curved body like a gear wheel under a resonance machine with uniaxial force application?



Tooth root fatigue strength

Involute Function

- How can we clamp a curved body like a gear wheel under a resonance machine with uniaxial force application?



Tooth root fatigue strength

Determination of the tooth root load carrying capacity

- S/N-Curve:
 - Correlation between load and number of load cycles

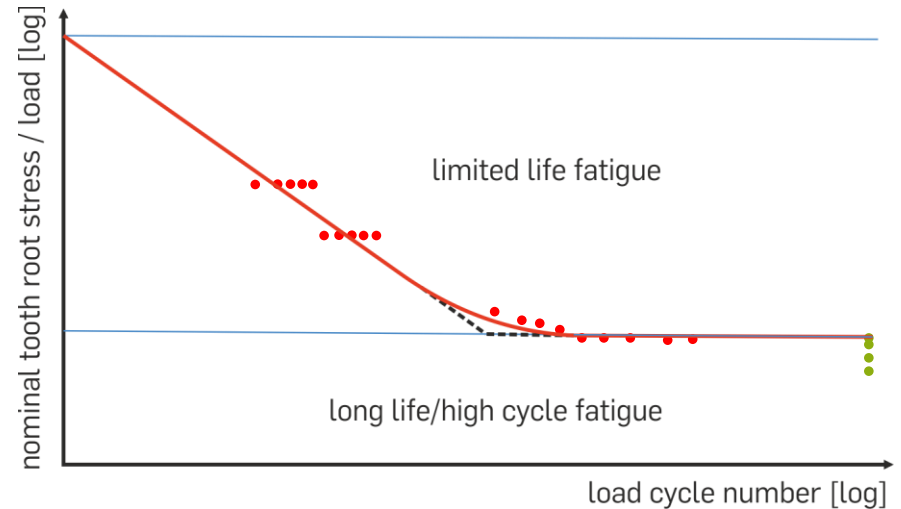
Procedure:

1. Determination of long life/high cycle fatigue

Staircase - Method

2. Determination of limited life fatigue

Horizon - Method

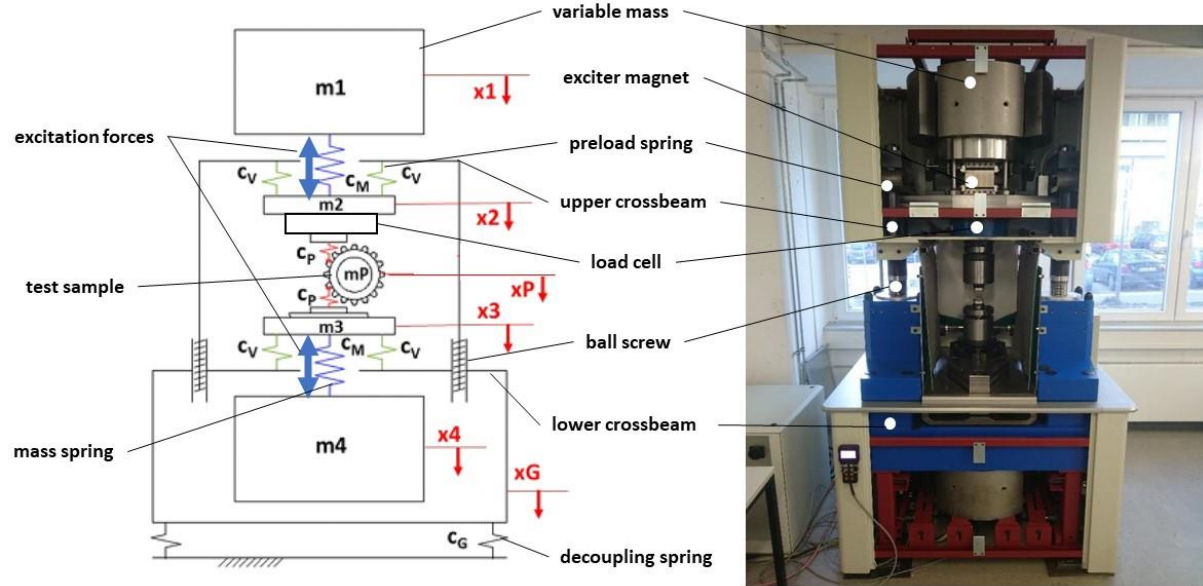


Test rig

Rumul VIBROFORTE 500

Electro-magnetically excited high-load resonance pulsator

- Test frequency $f_p = 50 - 160 \text{ Hz}$
- Max. force $F_{\max} = 500 \text{ kN}$
- Stat. force $F_{\text{stat}} = \pm 500 \text{ kN}$
- Dyn. force $F_{\text{dyn}} = \pm 250 \text{ kN}$
- Max. stroke $s_{\max} = \pm 2 \text{ mm}$



Variety of test specimens

$100 \text{ mm} < d_a < 500 \text{ mm}$



$d_a < 100 \text{ mm}$

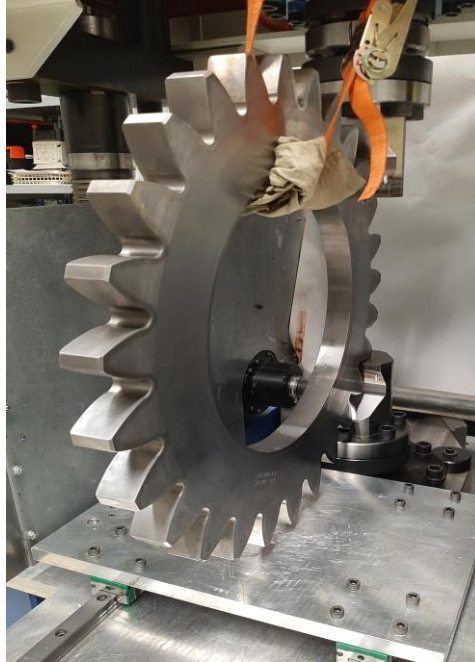


Specimen true to scale

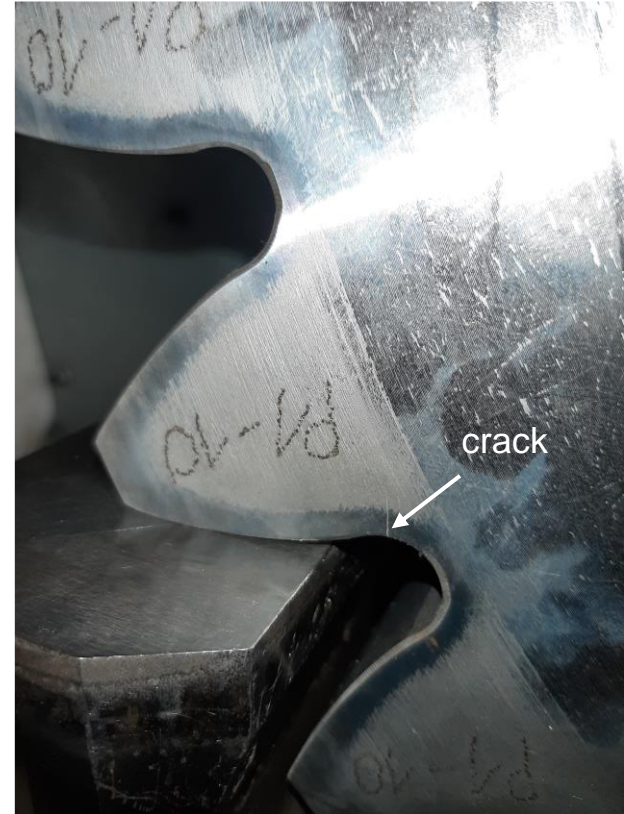
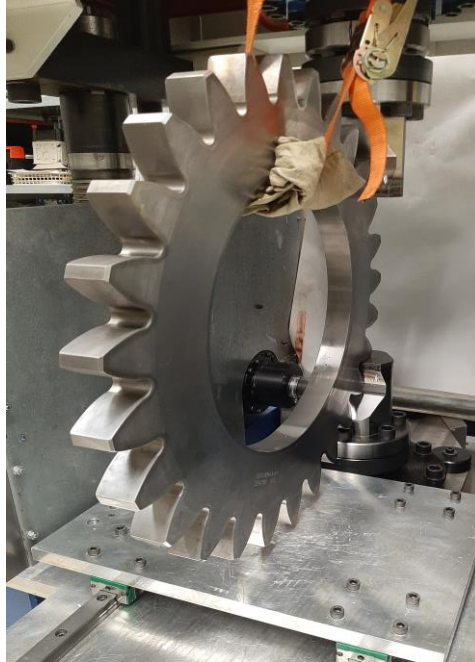
$d_a > 500 \text{ mm}$



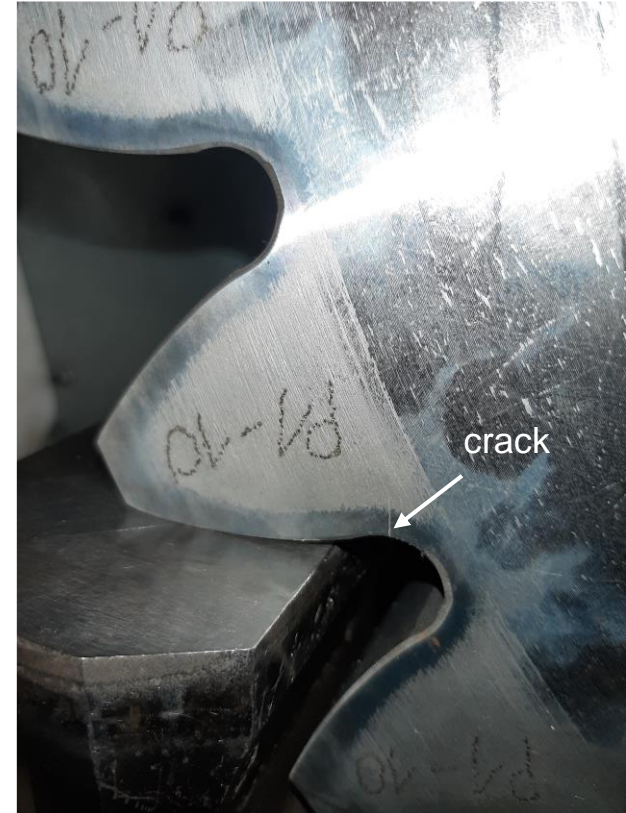
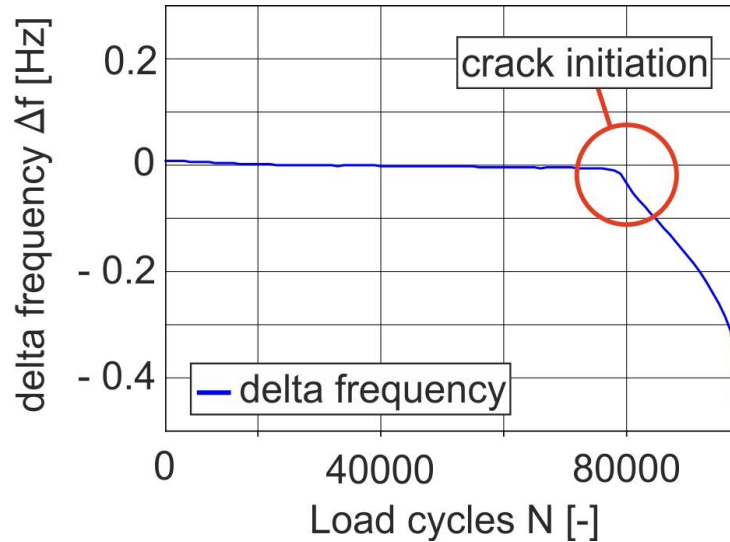
Test examples



Test examples

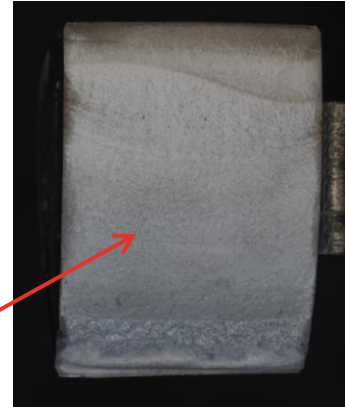


Test examples



Crack and fracture surface investigation

- Crack: Localization of the crack in the tooth root fillet
- Surface:
 - Heat treatment
 - Crack starting point/propagation
 - Material condition: e.g. ductility

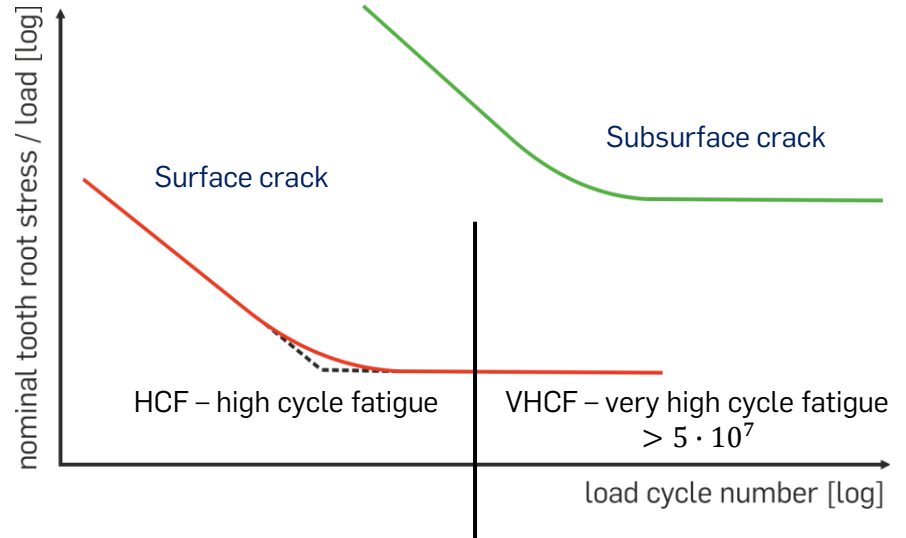


Outlook – Research on Gears

Research in the very high cycle fatigue

- allows the investigation of failure due to subsurface cracks
- provides higher in depth material knowledge
- allows a design for higher power density for longer time

How can we test the tooth root fatigue strength of gears for such high number of load cycles?



Outlook – Research on Gears

HCF – High cycle fatigue

$$N = 6 \cdot 10^6$$



$$n_{pulsator} = 100 \text{ Hz}$$

$$n_{running} = 1500 \text{ rpm} = 25 \text{ Hz}$$



$$t_{pulsator} = 16.6 \text{ H}$$

$$t_{running} = 66.6 \text{ H}$$

VHCF – Very high cycle fatigue

$$N = 5 \cdot 10^7$$



$$n_{pulsator} = 100 \text{ Hz}$$

$$n_{running} = 1500 \text{ rpm} = 25 \text{ Hz}$$



$$t_{pulsator} = 138.8 \text{ H} = 5.79 \text{ days}$$

$$t_{running} = 555.6 \text{ H} = 23.15 \text{ days}$$

How can we test the tooth root fatigue strength of gears for such high number of load cycles?

Outlook – Research on Gears

GIGAFORTE 50

Die GIGAFORTE 50 wurde speziell für Versuche im VHCF Bereich entwickelt. Mit einer Prüffrequenz von 1000 Hz können Versuche mit mehr als 100 Millionen Lastwechsel in kurzer Zeit gefahren werden. Es können Standardproben und kleine Bauteile kraft- oder dehnungsgeregelt zyklisch belastet werden.

Technische Daten

| | |
|-------------------------------------|--|
| <i>Max. Scheitelwert der Kraft</i> | 50 kN Zug/Druck |
| <i>Max. Schwingbreite der Kraft</i> | 50 kN (+/- 25 kN) |
| <i>Max. statische Kraft</i> | +/- 50 kN |
| <i>Dynamischer Weg</i> | 0,2 mm (+/- 0,1 mm) |
| <i>Prüffrequenz</i> | ca. 1000 Hz (+/- ca. 3 % abhängig von der Probensteifigkeit) |



GIGAFORTE 50

$$N = 5 \cdot 10^7$$



$$n_{Gigaforte} = 1000 \text{ Hz}$$



$$t_{Gigaforte} = 13.8 \text{ H} = 0.58 \text{ days}$$

$$t_{Pulsator} = 138.8 \text{ H} = 5.79 \text{ days}$$

$$t_{running} = 555.6 \text{ H} = 23.15 \text{ days}$$

Thank you for your attention

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